

# The optimality box in uncertain data for minimizing the sum of the weighted completion times of the given jobs

Y. N. Sotskov (Foreign) <sup>1</sup>,

T.-C. Lai <sup>2</sup>,

N. G. Egorova <sup>3</sup>

Frank Werner (Foreign) <sup>4</sup>

2017 г.

1, 2, 4 Foreign

<sup>3</sup> Belarusian State University of Informatics and Radioelectronics, Minsk,  
Belarus

**Keywords:** Single-machine scheduling, Uncertain processing times,  
Optimality box.

**Abstract:** An uncertain single-machine scheduling problem is considered, where the processing time of a job can take any real value from a given segment. The criterion is to minimize the total weighted completion time of the  $n$  jobs, a weight being associated with each given job. We use the optimality box as a stability measure of the optimal schedule and derive an  $O(n)$ -algorithm for calculating the optimality box for a fixed permutation of the given jobs. We investigate properties of the optimality box using blocks of the jobs. If each job belongs to a single block, then the largest optimality box may be constructed in  $O(n \log n)$  time. For the general case, we apply dynamic programming for

constructing a job permutation with the largest optimality box. The computational results for finding a permutation with the largest optimality box show that such a permutation is close to an optimal one, which can be determined after completing the jobs when their processing times became known.

**Published in:** Magdeburg, 2017. – 23 p. – (Preprint / Otto-von-Guericke-Universität; №1)