

- визуализация и копирование готового кода;
- добавление в графическое отображение различных элементов;
- преобразование графического отображения в интерактивную модель на основе определения необходимых элементов управления, набора данных, изменяемых переменных, начальных значений, диапазонов изменений значений.
- оформление интерактивной модели;
- преобразование интерактивной модели в формат CDF.

Интерактивные модели, полученные в результате символьных вычислений моделирует различные аспекты Textual Analysis и School Language Arts и могут быть использованы в иллюстративном качестве для исследовательской или образовательной деятельности, они также могут представлять интерес в качестве объектов изучения и основы для собственного лингвистического моделирования на основе символьных вычислений, особенно в контексте преподавания компьютерной лингвистики для студентов гуманитарных специальностей.

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#### ON P-NONINVARIANT EQUATION FOR SPIN 1/2 PARTICLE WITH ANOMALOUS MAGNETIC MOMENT

We start from the following spin-tensor system (let  $\hat{\partial} = \partial_\mu \gamma_\mu$ )

$$\begin{aligned}
 i\gamma_5 \left\{ b_1 \hat{\partial}(\gamma_\mu \Psi_\mu) - \frac{4b_2}{\sqrt{6}} \left[ -\frac{1}{4} \hat{\partial}(\gamma_\mu \Psi_\mu) + (\partial_\mu \Psi_\mu) \right] \right\} + M(\gamma_\mu \Psi_\mu) &= 0, \\
 i\gamma_5 \left\{ b_3 \hat{\partial} \Psi_0 - i \frac{4b_4}{\sqrt{6}} \left[ (\partial_\mu \Psi_\mu) - \frac{1}{4} \hat{\partial}(\gamma_\mu \Psi_\mu) \right] \right\} + M \Psi_0 &= 0, \\
 \frac{2i}{\sqrt{6}} \gamma_5 \left\{ b_5 \left[ \partial_\lambda (\gamma_\mu \Psi_\mu) - \frac{1}{4} \gamma_\lambda \hat{\partial}(\gamma_\mu \Psi_\mu) \right] - \right. \\
 \left. - ib_6 \left[ \partial_\lambda \Psi_0 - \frac{1}{4} \gamma_\lambda \hat{\partial} \Psi_0 \right] + M \left\{ \Psi_\lambda - \frac{1}{4} \gamma_\lambda (\gamma_\mu \Psi_\mu) \right\} \right\} &= 0, \tag{1}
 \end{aligned}$$

where parameters  $b_i$  obey restrictions

$$b_1 + b_3 = 1, \quad b_1 b_3 - b_2 b_5 - b_4 b_6 = 0, \quad b_2 b_3 b_5 + b_1 b_4 b_6 = 0.$$

These equations describe a particle with spin 1/2 and some additional intrinsic structure. From this equation, for the main bispinor component

$$\Phi(x) = b_5 \gamma_\mu \Psi_\mu(x) - ib_6 \Psi_0(x)$$

a modified Dirac-like  $P$ -noninvariant equation was found

$$\left\{ i\gamma_5 (\gamma_\mu \partial_\nu) + M \right\} \Phi(x) = 0.$$

Concomitant bispinors (see (1)) may be constructed through the main component

$$\gamma_\mu \Psi_\mu(x) = \frac{b_1^2}{b_5(b_1^2 - b_3^2)} \Phi(x), \quad \Psi_0(x) = \frac{-ib_3^2}{b_6(b_1^2 - b_3^2)} \Phi(x).$$

In presence of electromagnetic fields, the component  $\Phi(x)$  is the same, and it obeys the following  $P$ -noninvariant equation for a particle with anomalous magnetic moment

$$\left\{ i\gamma^5 \gamma_\mu (\partial_\mu + ieA_\nu) - \frac{4b_1 b_3}{M} ieF_{\mu\nu} \frac{\gamma_\mu \gamma_\nu - \gamma_\nu \gamma_\mu}{4} + M \right\} \Psi = 0.$$

Expressions for  $\Psi_0(x)$  and  $(\gamma_\mu \Psi_\mu)$  are

$$\begin{aligned} (\gamma_\mu \Psi_\mu) &= \frac{b_1^2}{b_5(b_1^2 - b_3^2)} \left\{ 1 + \frac{4}{3} \left( \frac{b_1 b_3}{M} \right)^2 ieF_{\mu\nu} \frac{\gamma_\mu \gamma_\nu - \gamma_\nu \gamma_\mu}{4} \right\} \Phi, \\ \Psi_0(x) &= -i \frac{b_3^2}{b_6(b_1^2 - b_3^2)} \left\{ 1 + \frac{4}{3} \left( \frac{b_1 b_3}{M} \right)^2 ieF_{\mu\nu} \frac{\gamma_\mu \gamma_\nu - \gamma_\nu \gamma_\mu}{4} \right\} \Phi. \end{aligned}$$

In order to follow extension of the model from flat Minkowski space to any Riemannian space-time we should make several modifications. In Riemannian space we use the metric  $g_{\alpha\beta}(x)$ , so we must make the change:  $M \rightarrow iM$ , and use Dirac matrices  $\gamma^a$ . Derivatives are modified according to the rules

$$D_\alpha(x) = \nabla_\alpha + \Gamma_\alpha(x) + ieA_\alpha(x), \quad \hat{D} = \gamma^\alpha(x) D_\alpha(x),$$

where  $\Gamma_\alpha(x)$  is bispinor connection, and  $\gamma^\alpha(x) = \gamma^a e_{(a)}^\alpha(x)$ . Note needed relations

$$\begin{aligned} \hat{D}(x) &= \gamma^\rho(x) D_\rho = D_\beta \gamma^\rho(x), \quad D_\sigma(x) g_{\alpha\beta}(x) = g_{\alpha\beta}(x) D_\sigma(x), \\ \hat{D}\hat{D} &= D^\alpha D_\alpha - \Sigma(x), \quad \Sigma(x) = -ieF_{\alpha\beta} \sigma^{\alpha\beta}(x) + \frac{R}{4}, \end{aligned}$$

where  $R(x)$  is the Ricci scalar. Recall the definitions for  $\gamma^5$ -matrix:

$$\begin{aligned} \gamma^5(x) &= \frac{i}{4!} \varepsilon_{\alpha\beta\rho\sigma}(x) \gamma^\alpha(x) \gamma^\beta(x) \gamma^\rho(x) \gamma^\sigma(x), \\ \varepsilon^{\alpha\beta\rho\sigma}(x) &= \varepsilon^{abcd} e_{(a)}^\alpha(x) e_{(b)}^\beta(x) e_{(c)}^\rho(x) e_{(d)}^\sigma(x), \quad \varepsilon_{0123} = -1. \end{aligned}$$

Levi-Civita object  $\varepsilon^{\alpha\beta\rho\sigma}(x)$  changes under tetrad transformations as follows

$$\varepsilon^{\alpha\beta\rho\sigma}(x) = \det[L_a^b(x)] \varepsilon^{abcd}(x).$$

In particular, at the tetrad  $P$ -reflection, it transforms as a tetrad pseudoscalar. Analysis for the generally covariant system remains in fact the same. We write down final results:

$$\Phi = b_5(\gamma_\mu \Psi_\mu) - ib_6 \Psi_0,$$

$$\left\{ i\gamma^5(x) \hat{D}(x) - \frac{4b_1 b_3}{M} \left[ -ieF_{\mu\nu} \sigma^{\mu\nu}(x) + \frac{R(x)}{4} \right] + iM \right\} \Phi = 0.$$

Expressions for concomitant components are given by the generally covariant formulas

$$\begin{aligned} \gamma^\mu(x) \Psi_\mu(x) &= \frac{b_1^2}{b_5(b_1^2 - b_3^2)} \left\{ 1 - \frac{4}{3} \left( \frac{b_1 b_3}{iM} \right)^2 \left( -ieF_{\mu\nu} \sigma^{\mu\nu} + \frac{R(x)}{4} \right) \right\} \Phi, \\ \Psi_0(x) &= -i \frac{b_3^2}{b_6(b_1^2 - b_3^2)} \left\{ 1 - \frac{4}{3} \left( \frac{b_1 b_3}{iM} \right)^2 \left( -ieF_{\mu\nu} \sigma^{\mu\nu} + \frac{R(x)}{4} \right) \right\} \Phi. \end{aligned}$$

This theory gives a  $P$ -noninvariant model for spin 1/2 particle with anomalous magnetic moment in presence of external fields, electromagnetic and gravitational.